

Pricing Inequality

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Federal Reserve Bank of Minneapolis - December 2022

The views expressed herein are those of the authors and not those of the Federal Reserve System.

Introduction

Core idea of this paper

Household wealth and income → *Sensitivity to differences in prices* → *Price setting*

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Motivating example 1 - *Auer Burstein Lein Vogel (2022)*

- Swiss Franc appreciation
- **Main result** - *Higher income households* → ? → *Lower substitution toward French goods*

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- Increase in local house prices
- **Main result** - *Areas with more owners* → ? → *Larger increases in markups on goods*

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- Increase in local house prices
- **Main result** - *Areas with more owners* → ? → *Larger increases in markups on goods*

Scenario 1 - Poor households receive large increase in transfers

Scenario 2 - Firms selling to poor households hit with a cost shock

Welfare - How do prices change? How is expenditure reallocated?

Today

1. Theory

- Incomplete markets + Extensive margin demand in general equilibrium
Bewley, Aiyagari, Hugget Multinomial logit
- Characterize (i) price elasticities of demand, (ii) sorting, (iii) pass-through

2. Numerical example

- Counterfactual 1 - Lump sum transfer financed by an increase in marginal income tax
 - *Reduction in demand elasticities of most elastic households → Higher markups*
- Counterfactual 2 - Marginal cost shock to all / some firms
 - *Rich households' decline in welfare is insulated by trading down to cheaper varieties*

Environment

Differentiated goods - Goods $g \in \mathcal{G}$. Each good produced by J firms $j \in \{1, \dots, J\}$

$$y_{jgt} = \bar{Z}_d z_{jg} n_{jgt} \quad , \quad z_{jg} \sim \Gamma_z(z)$$

Homogeneous goods - Continuum of identical firms

$$Y_{ct} = \bar{Z}_c N_{ct}.$$

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Households - Continuum of households $i \in [0, 1]$

- Stochastic productivity e_t^i : $e_{it+1}^i \sim \Gamma_e(e|e_t^i)$
- Each period choose a good g and producer j , and purchase one unit from them

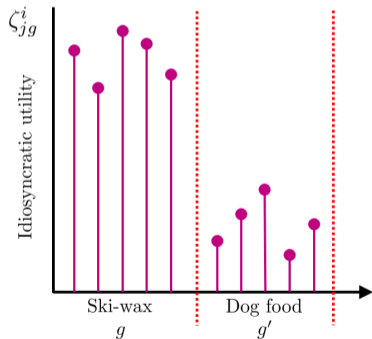
$$\mathbb{E}_0 \left[\sum_{t=0}^{\infty} \beta^t \tilde{u}_{jgt}^i \right] \quad , \quad \tilde{u}_{jgt}^i = \underbrace{u(c_t^i)}_{\text{Homog. good}} + \underbrace{\zeta_{jgt}^i}_{\text{Diff. good}} \quad , \quad \underbrace{\zeta_t^i}_{\text{iid each period}} \sim \Gamma_\zeta(\zeta)$$

- Savings a_t^i in government debt, interest rate r , borrowing constraint $a_{t+1}^i \geq \underline{a}$.

Environment - Preferences - Nested Gumbel

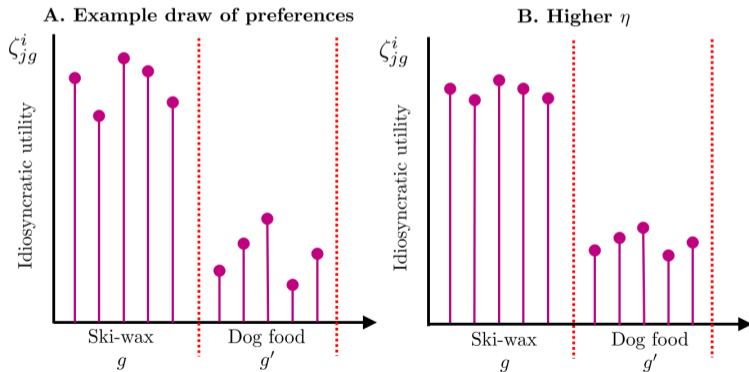
$$\zeta^i \sim \Gamma_{\zeta}(\zeta^i) = \prod_{g \in \mathcal{G}} \exp \left\{ - \left(\sum_{j \in g} e^{-\eta \zeta_{jg}^i} \right)^{\theta/\eta} \right\}$$

A. Example draw of preferences



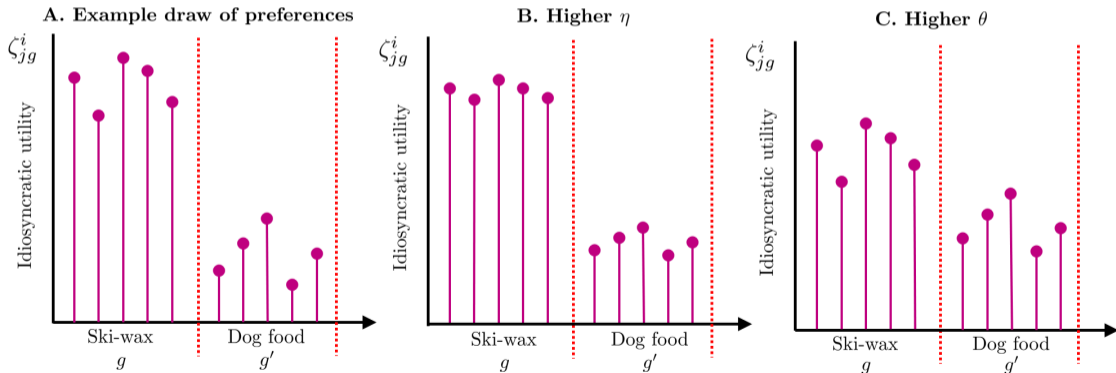
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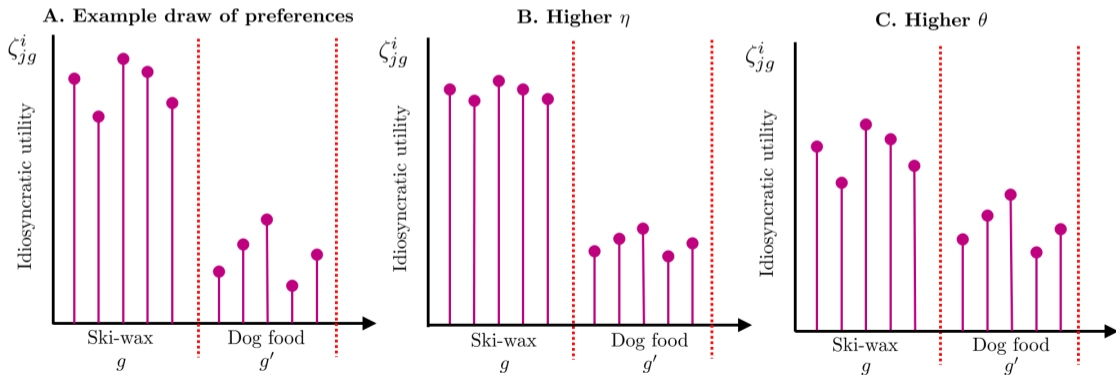
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Environment - Preferences - Nested Gumbel

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Household problem

1. Given all prices p_{jg} and preferences ζ_{jg} , choice over goods g and producers j

$$\bar{V}(a, e) := \mathbb{E}_{\zeta} \left[\max_{j, g} \left\{ V(a, e, p_{jg}) + \zeta_{jg} \right\} \right]$$

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2. Conditional on choosing firm p_{jg} , and given W, r, Π , choose consumption/savings

$$V(a, e, p_{jg}) = \max_{a', c} u(c) + \beta \int \bar{V}(a', e') d\Gamma_e(e'|e)$$

$$P_c c + p_{jg} + a' = (1 - \tau) W e + (1 + r) a + \Pi$$

$$a' \geq \underline{a}$$

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$$P_c c + p_{jg} + a' = (1 - \tau) W e + (1 + r) a + \Pi \quad , \quad \frac{\partial V(a, e, p_{jg})}{\partial p_{jg}} = -\Lambda(a, e, p_{jg})$$
$$a' \geq \underline{a}$$

Firm problem

Given *Competitors' Prices* \mathbf{p}_g and *Aggregates*, choose *Price* p_{jg} to maximize profits

$$p_{jg}^* = \arg \max_{p_{jg}} \underbrace{x(p_{jg}, \mathbf{p}_g, \mathbf{S})}_{\text{Demand}} \underbrace{\left(p_{jg} - \frac{W}{Z_d z_{jg}} \right)}_{\text{Per unit profit}}$$

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Demand - The equilibrium quantity sold is

$$x(p_{jg}, \mathbf{p}_g, \mathbf{S}) = \int_{A \times E} \rho(a, e, p_{jg}, \mathbf{p}_g, \mathbf{S}) d\Gamma_{a,e}(a, e)$$
$$\rho(a, e, p_{jg}, \mathbf{p}_g, \mathbf{S}) = \frac{e^{\eta V(a, e, p_{jg})}}{e^{\eta \tilde{V}(a, e, p_{jg}, \mathbf{p}_g)}} \times \frac{e^{\theta \tilde{V}(a, e, p_{jg}, \mathbf{p}_g)}}{e^{\theta \bar{V}(a, e)}}$$

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Demand - The equilibrium quantity sold is

$$x_{jg} = \int \rho_{jg}^i di$$
$$\rho_{jg}^i = \rho_{j|g}^i \rho_g^i = \frac{e^{\eta V^i(p_{jg})}}{e^{\eta \tilde{V}^i(\mathbf{p}_g)}} \frac{e^{\theta \tilde{V}^i(\mathbf{p}_g)}}{e^{\theta \bar{V}^i}}$$

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Optimality / Nash - Standard markup condition

$$p_{jg}^* = \underbrace{\frac{\epsilon_{jg}}{\epsilon_{jg} - 1}}_{\text{Markup}} \underbrace{\frac{W}{\bar{Z}_d z_{jg}}}_{\text{Marginal cost}}$$

$$\epsilon_{jg} = - \left. \frac{\partial \log x_{jg}}{\partial \log p_{jg}} \right|_{\mathbf{p}_{-jg}^*}$$

▸ Details - Second order conditions

Next couple of slides

Key objects for welfare effect of a change in marginal cost to firm jg :

1. *How do prices change?*

Pass-through: $\frac{\partial \log p_{jg}}{\partial \log mc_{jg}}$

2. *Who does it affect?*

Sorting: ρ_{jg}^i , $\frac{\partial \log \rho_{jg}^i}{\partial a^i}$

3. *How does spending reallocate?*

Elasticities: $\epsilon_{jg}^i = -\frac{\partial \log \rho_{jg}^i}{\partial \log p_j}$, $\epsilon_{jg} = -\frac{\partial \log x_{jg}}{\partial \log p_j}$

1. Elasticity of demand

Recap: $\rho_{jg}^i = \frac{e^{\eta V^i(p_{jg})}}{e^{\eta \tilde{V}^i(\mathbf{p}_g)}} \frac{e^{\theta \tilde{V}^i(\mathbf{p}_g)}}{e^{\theta \bar{V}^i}}$, $\tilde{V}^i(\mathbf{p}_g) = \frac{1}{\eta} \log \left[\sum_{k \in g} e^{\eta V^i(p_{kg})} \right]$, $x_{jg} = \int \rho_{jg}^i di$

Individual demand: $\rho_{j|g}^i \rho_g^i$ Market g value Firm demand

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Result 1: Price elasticity decreases in wealth and income

- **Poor:** Higher $u'(c_{jg}^i)$, higher ε_{jg}^i , driven by switching across products
- **Bewley:** Rich model for the endogenous distribution of $u'(c_{jg}^i)$ or, equivalently, V_a^i

2. Sorting

Result 2: High price firms sell more to wealthy households

Fix prices \mathbf{p}_g , do *conditional* choices probabilities $\rho_{j|g}^i$ increase or decrease in a^i ?

$$\log \rho_{j|g}^i = \eta \left\{ V^i(p_{jg}) - \tilde{V}^i(\mathbf{p}_g) \right\}, \quad \frac{\partial \log \rho_{j|g}^i}{\partial a^i} = \eta \left\{ V_a^i(p_{jg}) - \mathbb{E}_{\rho_{k|g}^i} \left[V_a^i(p_{kg}) \right] \right\}$$

- (+) If j has a high price, then the marginal value of resources is high if buy from j
 - For a high price firm, its customer base is *increasing* in assets

- (-) If j has a low price, then marginal value of resources is low if buy from j
 - For a low price firm, its customer base is *decreasing* in assets

3. Pass-through

Result 3: Off-setting forces shape pass-through

▶ Compare to Nevo (2000) version of BLP (1995)

$$p_{jg} = \frac{\varepsilon_{jg}}{\varepsilon_{jg} - 1} mc_{jg} \quad , \quad \frac{\partial \log p_{jg}}{\partial \log mc_{jg}} = \frac{[\varepsilon_{jg} - 1]}{[\varepsilon_{jg} - 1] + \left\{ \frac{\partial \log \varepsilon_{jg}}{\partial \log p_{jg}} \right\}_{(+)}} \in (0, 1)$$

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Recap: $\varepsilon_{jg} = \int \left[\eta(1 - \rho_{j|g}^i) + \theta \rho_{j|g}^i \right] p_{jg} u'(c_{jg}^i) \left(\frac{\rho_{jg}^i}{x_{jg}} \right) di$

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$$\frac{\partial \log \varepsilon_{jg}}{\partial \log p_{jg}} = \underbrace{\mathbb{E} \left[\frac{\eta(\eta - \theta) \rho_{j|g}^i (1 - \rho_{j|g}^i)}{\eta(1 - \rho_{j|g}^i) + \theta \rho_{j|g}^i} p_{jg} u'(c_{jg}^i) \right]}_{1. \text{ Market share effect}} \underbrace{+ 1 + \sigma \mathbb{E} \left[mpc_{jg}^i \left(\frac{p_{jg}}{c_{jg}^i} \right) \right]}_{2. \text{ Elasticity effect}} \underbrace{- \mathbb{V} \left[\frac{\varepsilon_{jg}^i}{\varepsilon_{jg}} \right]}_{3. \text{ Composition effect}}$$

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- Here pass-through is endogenous ... and ambiguous:

(+) Lose quantity, smaller share, increases elasticity

(+) Make all consumers more price elastic. More so if high MPC, or high expenditure share on j

(-) Lose high elasticity buyers first, reduces overall elasticity

Direct evidence on substitution of poor / rich households

Model

$$\text{Budget share: } b_{ijt} = \frac{p_{jt} \phi_{jt} \exp \{ \eta V_i(p_{jt}) \}}{\sum_k p_{kt} \phi_{kt} \exp \{ \eta V_i(p_{kt}) \}}$$
$$\log \left(\frac{b_{ijt}}{b_{ikt}} \right) - \log \left(\frac{b_{mjt}}{b_{mkt}} \right) \approx \underbrace{\left\{ \varepsilon_{ikt} \right\} \left\{ \sigma \right\} \left\{ \frac{\partial \log c_i(p_{kt})}{\partial \log e_i} \right\}}_{\text{Coefficient estimated in Auer et al (2022)}} \underbrace{\log \left(\frac{e_i}{e_m} \right) \log \left(\frac{p_{jt}}{p_{kt}} \right)}_{\text{Interaction term}}$$

Data

$$\log \left(\frac{b_{it}^M}{b_{it}^D} \right) = \beta_0 - \beta_1 \log \left(\frac{p_t^M}{p_t^D} \right) + \beta_2 \log e_i \log \left(\frac{p_t^M}{p_t^D} \right) + \varepsilon_{it} \quad , \quad \hat{\beta}_2 = 2.2$$

Auer et al (2022) - *Unequal Expenditure Switching: Evidence from Switzerland*

► Restriction on σ, ε under Auer et al (2022) estimate

NUMERICAL EXAMPLE

Simplifying assumption: $\theta = \eta$

Calibration - Quarterly - 1/2

Key parameters

- η such that average markup is 1.20
- \bar{Z}_d such that 15% of spending on differentiated good
- Close to log preferences $\sigma = 1.50$

Income

- AR(1) in income, only persistent shocks for now

$$\log e_{it+1} = \rho_e \log e_{it} + \varepsilon_{it+1} \quad , \quad \varepsilon_{it+1} \sim \mathcal{N} \left(-\frac{1}{2} \frac{v_e^2}{1 + v_e}, v^2 \right)$$

- Krueger Perri Mitman (2016) - $\rho_e = 0.99$, $v_e = 0.023$ No transitory shocks, same $\text{var}(\log y_{it})$

Calibration - Quarterly - 2/2 - Wealth and general equilibrium

- GE version of the 'Liquid wealth' calibration in Kaplan Violante (2022)
- Average liquid wealth to average income $\mathbb{E}[a_i]/\mathbb{E}[y_i] = 0.56$ (SCF)
- Borrowing constraint $\underline{a} = 0$ and baseline annual $r = 0.02$

- Demand for debt:

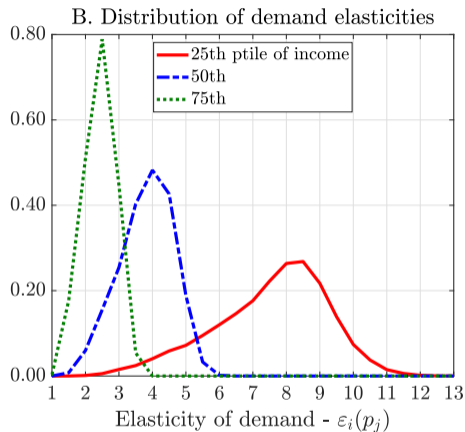
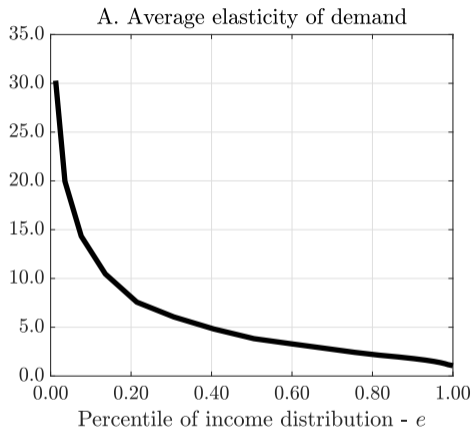
$$B^d(r) = \frac{T - G}{r} \quad , \quad T = \tau \int W e_i d i \quad , \quad \tau = 0.20$$

- Supply of debt:

$$B^s(r) = \int a d\lambda(a, e)$$

- Calibrate $\beta = 0.92$ ($r_{RA} = 38\%$) to give 0.56. Implies $G/Y = 0.19$. In US ≈ 0.30
- Implies a quarterly MPC out of \$500 of 16.9%

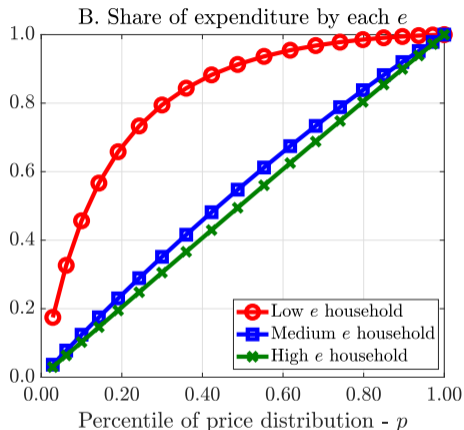
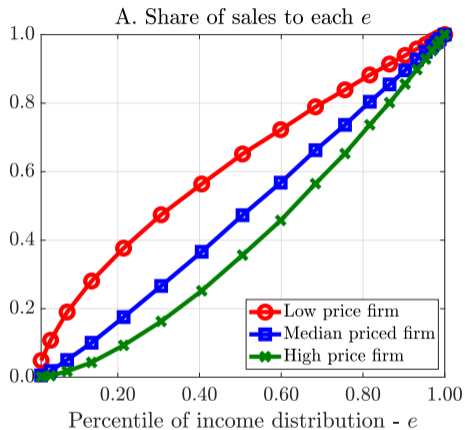
1. Elasticities - $\varepsilon(a, e, p_j)$



- Cross-sectional regression in same form as interaction terms in Auer et al (2022)

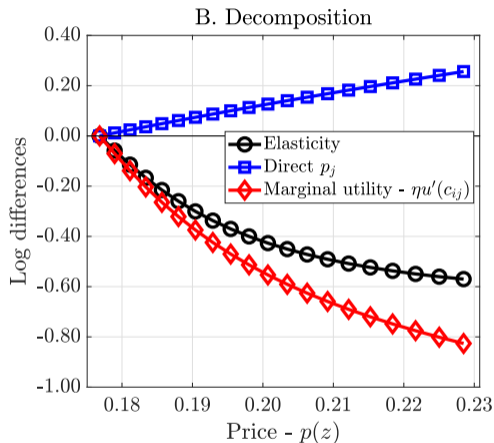
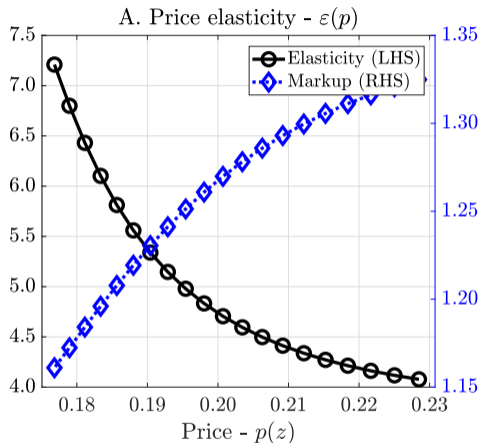
$$\varepsilon_j = \alpha - 6.25 \log \text{Income}_j \quad , \quad \text{overstates their estimate of } -2.19$$

2. Sorting - $\rho(a, e, p_j)$



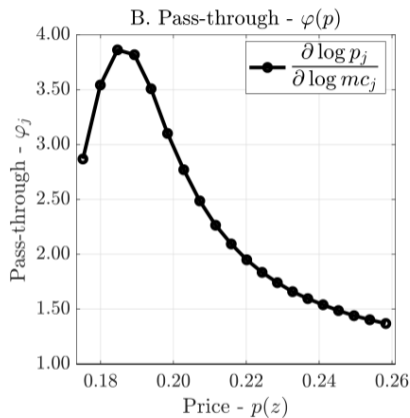
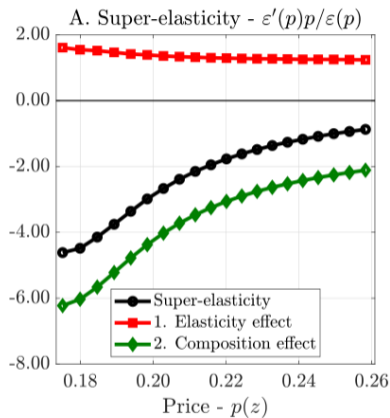
- At **low priced firms**, more than **60 percent** of sales to below median income households
- At **high priced firms**, less than **40 percent** of sales to below median income households

3. Markups - μ_j



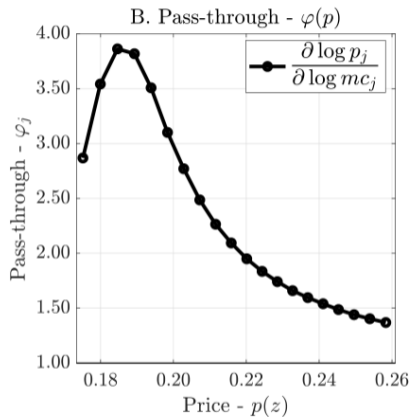
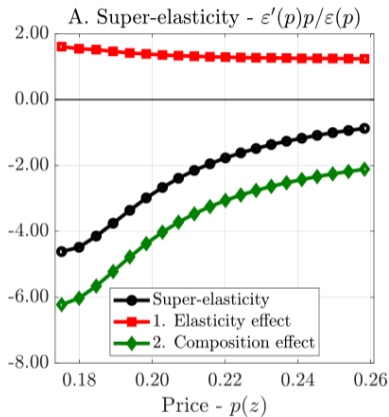
- Low price firms sell to poorer households, operate with lower price-cost margins
- Consistent with Sanghani (2022) - *Markups Across the Income Distribution*

4. Pass-through - $\varphi(p_j)$



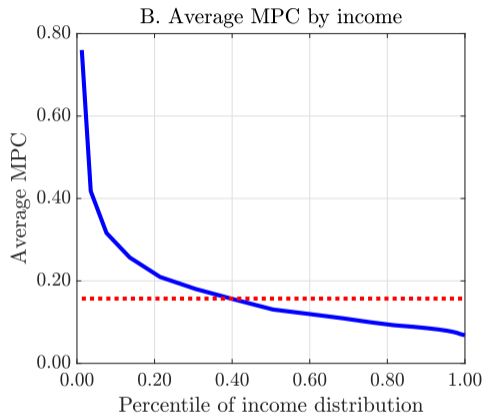
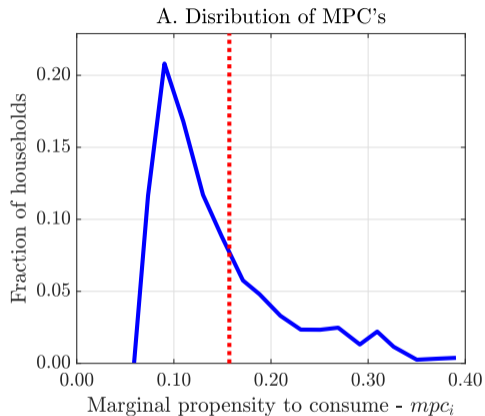
1. Low priced firms sell to higher MPC households, and p_j is a larger share of budget
2. More heterogeneity in buyers at low priced firms: $\uparrow CV[u'(c_{ij})]$

4. Pass-through - $\varphi(p_j)$



- Issue (i) Too much sorting, (ii) Too steep relationship between e_i and ε_i
- Optimistic This is fine, as we also miss the data in these directions too!

4. Pass-through - $\varphi(p_j)$ - Marginal propensities to consume



- Low priced firms sell to higher MPC consumers

Counterfactual 1 - Shock to costs

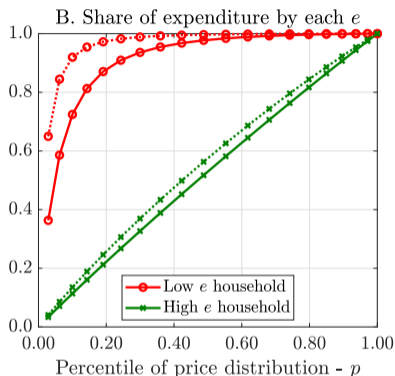
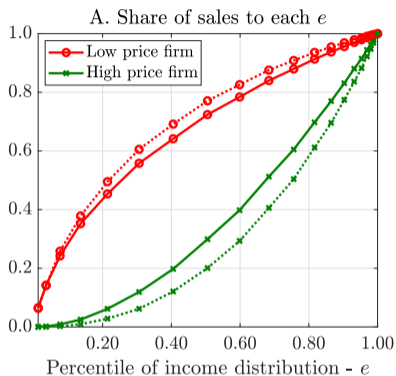
- Distributional change in prices in partial equilibrium (W , r and Π_d fixed)
 1. Decrease productivity of all differentiated goods. Raise prices by 30%
 2. Decrease productivity of cheap differentiated goods. Raise cheap prices by 30%
- What does the first order approximation of welfare effects miss?

$$\Delta \log V(a, e) \approx \sum_j b_j(a, e, p_j) \Delta \log p_j \quad \text{v.s.} \quad \Delta \log \bar{V}(a, e)$$

- First order welfare effects used as an empirical benchmark in leading studies

E.g. Borusyak, Jaravel (2021) - *Distributional Effects of Trade: Theory and Evidence from the United States*

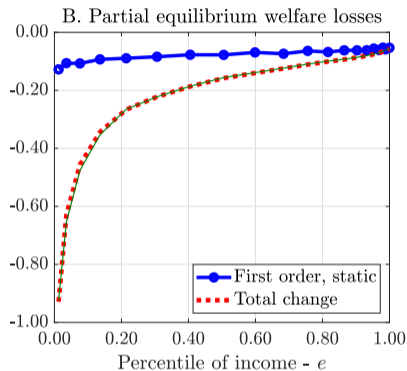
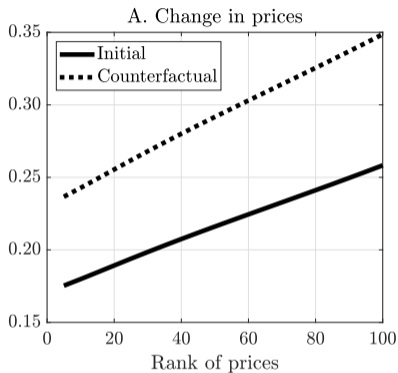
Counterfactual 1 - Shock to costs



- Trading down of high wealth consumers to cheaper products mitigates welfare losses
- Consistent with behavior in the Great Recession documented by [Argente Lee \(2021\)](#)

► Figure - Raise cheap goods prices by 30%

Counterfactual 1 - Shock to costs



- Trading down of high wealth consumers to cheaper products mitigates welfare losses
- Consistent with behavior in the Great Recession documented by [Argente Lee \(2021\)](#)

► Figure - Raise cheap goods prices by 30%

Combine standard models for pricing, consumption and savings

- Endogenous general equilibrium model for demand and pricing
- Refine, and then use for normative questions

1. Heterogeneity in inflation incidence across households in 2021/2022

- Are real wages really going up for poor households, or are their price indexes wiping out gains?
- Inflation in core categories of goods vs. in luxury goods

2. Targeted vs. Non-targeted transfers. What goes into prices? quantities?

- Transfers to poor, more elastic, more competitive product markets
- Transfers to rich, more inelastic, lower pass-through
- E.g. Stroebe Vavra (2019) - How changes in wealth feed into local prices

APPENDIX SLIDES

Previous approaches

1. Consumer demand - Low income households

- (i) Buy at low prices, markups Faber Fally (2022), Sanghani (2022)
- (ii) Have more elastic demand Apoorv Gupta (2021)
- (iii) Expenditure switch across goods Auer, Burstein, Lein, Vogel (2022)
- (iv) Experience larger price changes Jaravel, Sager (2021)

Non-homothetic CES: Matsuyama (2019), Handbury (2021), Comin, Lashkari, Mestieri (2021)

2. Firm pricing - The following seem to be correlated across firms:

- (i) Higher markups Burstein, Carvalho, Grassi (2022), Edmond, Midrigan Xu (2021)
- (ii) Lower pass-through Amiti, Itskhoki, Konnings (2019), Baqaee, Farhi, Sanghani (2021)

Homothetic Non-CES: Edmond Midrigan Xu (2021), Baqaee Farhi (2021), Boar Midrigan (2021), Bornstein Peters (2022)

▶ Back - Intro 1

▶ Back - Intro 2

Household problem - When choices are not feasible

- Cases of (a, e) in which setting $a' = \underline{a}$ and buying j implies $c < 0$:

$$(1 - \tau)We + (1 + r)a + \Pi - \underline{a} - p_j < 0$$

- Let $\mathcal{J}(a, e, \mathbf{p})$ be the set of all budget-feasible j
- Then choice is

$$\begin{aligned}\tilde{V}(a, e) &= \mathbb{E} \left[\max_{j \in \mathcal{J}(a, e, \mathbf{p})} \left\{ V(a, e, p_j) + \zeta_j \right\} \right], \quad \zeta \sim G(\zeta; \eta) \\ \rho(a, e, p_j) &= \frac{e^{\eta V(a, e, p_j)}}{\sum_{k \in \mathcal{J}(a, e, \mathbf{p})} e^{\eta V(a, e, p_k)}}\end{aligned}$$

1. Love-of-variety is valued:

$$\tilde{V}(a, e) = \frac{1}{\eta} \log \left(\sum_{j \in \mathcal{J}(a, e, \mathbf{p})} \exp \left\{ \eta V(a, e, p_j) \right\} \right) = \underbrace{\frac{1}{\eta} \log |\mathcal{J}(a, e, \mathbf{p})| + V(a, e, \bar{p})}_{\text{If for all } j \in \mathcal{J}(a, e, \mathbf{p}), \text{ then } p_j = \bar{p}}$$

2. Everyone buying Gucci can buy Walmart. Some can only buy from Walmart. Competitive: Walmart ignores this.

Household problem - Monotonicity and discounting

- Bellman equation

$$V(a, e, p_j) = \max_{a', c} u(c) + \beta \int \frac{1}{\eta} \log \left[\sum_k \exp \left\{ \eta V(a, e, p_k) \right\} \right] d\Gamma(e'|e)$$
$$P_c c + p_j + a' = (1 - \tau) W e + (1 + r) a + \Pi \quad , \quad a' \geq \underline{a}.$$

1. Discounting

$$\beta \int \frac{1}{\eta} \log \left[\sum_k \exp \left\{ \eta \left[V(a, e, p_k) + a \right] \right\} \right] d\Gamma(e'|e) = \beta \int \frac{1}{\eta} \log \left[\sum_k \exp \left\{ \eta V(a, e, p_k) \right\} \right] d\Gamma(e'|e) + \beta a$$

2. Monotonicity

- Transformations are monotonic

▶ Back - Household problem

Relationship with Fajgelbaum, Grossman, Helpman (JPE 2011)

Our paper

- Preferences

$$u_{ij} = v(c_{ij}, \phi_j) + \varepsilon_{ij} \quad , \quad v(c_{ij}, \phi_j) = u(c_{ij}) + \eta^{-1} \log \phi_j$$

- Demand elasticity

$$\varepsilon_j = \eta p_j \iint u'(c(a, e, p_j)) \omega_j(a, e) da de$$

FGH (2011)

- Preferences

$$u_{ij} = v(c_{ij}, \phi_j) + \varepsilon_{ij} \quad , \quad v(c_{ij}, \phi_j) = c_{ij} \phi_j$$

- Demand elasticity

$$\varepsilon_j = \eta p_j \phi_j \quad , \quad p_j = \frac{W}{z_j} + \frac{1}{\eta \phi_j} \quad , \quad \text{Choose } \eta(\phi), \text{ s.t. } \uparrow \phi, \downarrow \eta(\phi)$$

Firm problem - Second order conditions

- Definitions

$$\varepsilon_x(p) = -\frac{x'(p)p}{x(p)} \quad , \quad \varepsilon_{xx}(p) = -\frac{x''(p)p}{x'(p)} \quad , \quad \sigma_x(p) = \frac{\partial \log \varepsilon_x(p)}{\partial \log p}$$

- Second order condition

$$\begin{aligned} \varepsilon_{xx}(p) / \varepsilon_x(p) &< 2 \\ -\sigma_x(p) &< 2\varepsilon_x(p) + 1 \end{aligned}$$

- $\sigma_x(p) > 0$ - Sufficient condition is a *positive* super-elasticity

$$\uparrow p, \uparrow \varepsilon_x, \downarrow \mu, \downarrow p$$

- $\sigma_x(p) < 0$ - If the super-elasticity $\sigma_x(p)$ is *very negative* then

$$\uparrow p, \downarrow \varepsilon_x, \uparrow \mu, \uparrow p$$

- We check second order conditions in quantitative exercise

Key departure - Dynamic budgeting

Simon

Kjetil

Fabrizio

Goods

Today

BBQ tongs
 g'''

$p_{1g'''} , \dots , p_{Jg'''}$

Today

Ski wax
 g''

$p_{1g''} , \dots , p_{Jg''}$

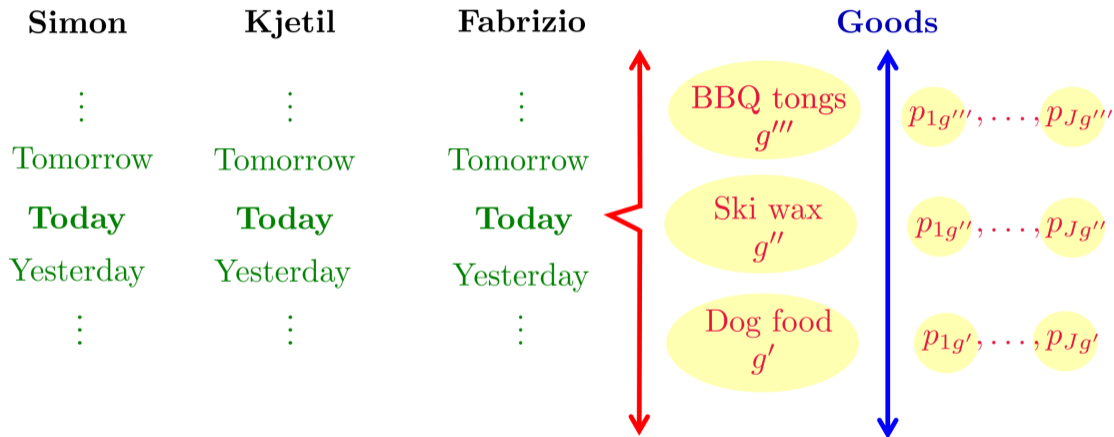
Today

Dog food
 g'

$p_{1g'} , \dots , p_{Jg'}$



Key departure - Two-stage budgeting - E.g. Nested CES / Kimball



E.g. Eeckhout, De Loecker, Mongey (2022), EMX (2022), Boar Midrigan (2021)

3. Pass-through - BLP

Nevo's (2000) interpretation of Berry, Levinsohn, Pakes (1995)

$$V(e_i, p_j) = \phi_j + \alpha_{e_i}(e_i - p_j) + \zeta_{ij}$$

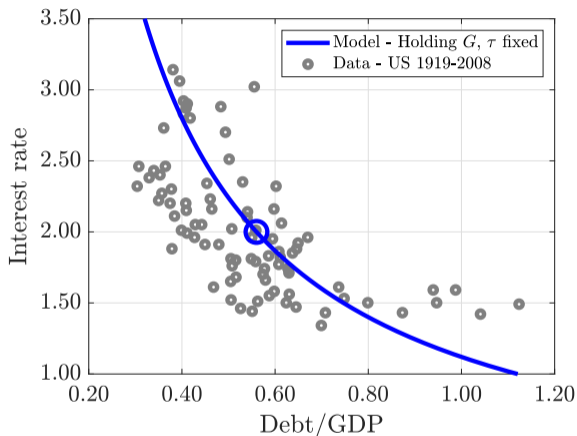
Then we have:

$$\varepsilon_j = \int \varepsilon_{ij} s_{ij} di, \quad \varepsilon_{ij} = \eta p_j \alpha_e, \quad s_{ij} = \frac{\rho_{ij}}{x_j}$$

$$\frac{\partial \log \varepsilon(p)}{\partial \log p} = \int \underbrace{\frac{\rho_{ij} \alpha_e}{\int \rho_{kj} \alpha_k dk}}_{\text{Elasticity weights}} \left[\underbrace{1}_{\text{1. Elasticity effect}} \quad \underbrace{- (\alpha_e - \varepsilon_j)}_{\text{2. Composition effect}} \right] di$$

- No effect via marginal value of left-over resources
- Distribution of elasticities (mostly) exogenous
- If $\alpha_e = \bar{\alpha}$, then super-elasticity is 1

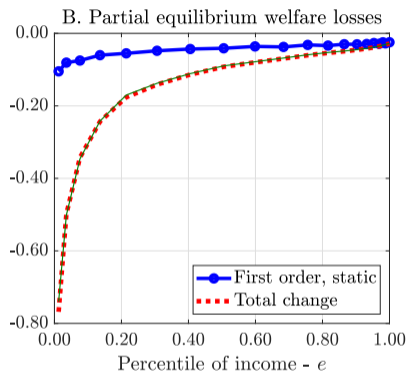
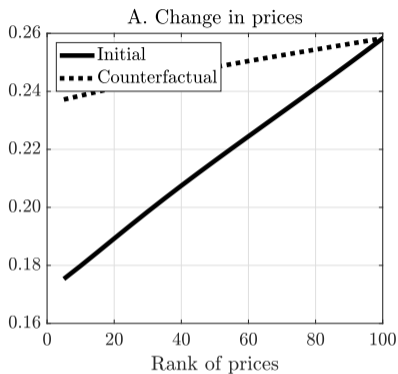
Debt-to-GDP and interest rates



- Krishnamurthy Vissing-Jorgensen (JPE, 2012) - *Aggregate Demand for Treasury Debt*

x-axis: Data mean of 0.43 adjusted to target $B = 0.56$, y-axis: Data mean spread of 8.1% adjusted to target 2%

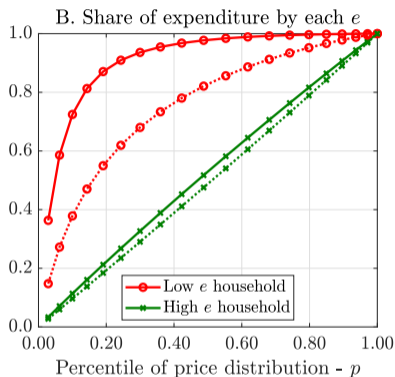
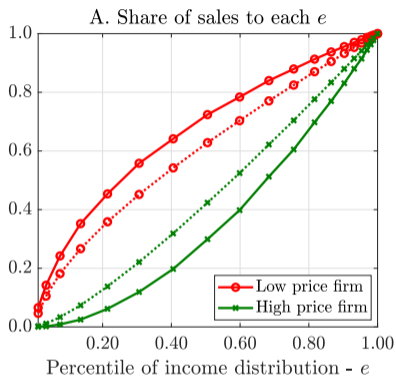
Counterfactual - Distorted productivity shock



- First order approximation still misses expenditure switching

▶ Back - Common price change

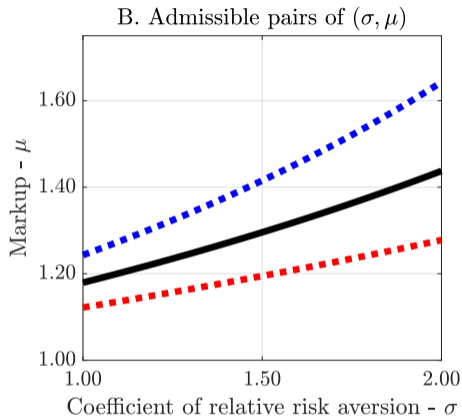
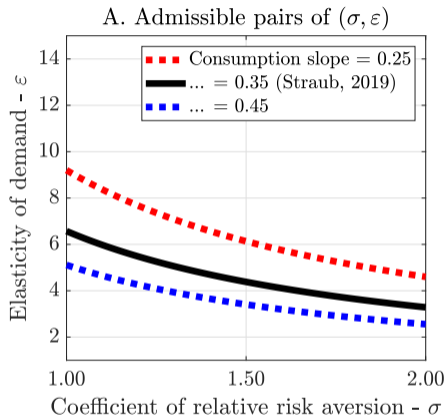
Counterfactual - Distorted productivity shock



- With higher price of cheap goods, both shift to higher priced goods.
- Rich, more so.

[▶ Back - Common price change](#)

Implied restriction on parameters



- Plot combinations of (σ, ε) that give $\varepsilon \times \sigma \times \frac{\partial \log c_i}{\partial \log y_i} = 2.2$

Calibration - Quarterly - 2/3 - Productivity and quality

- Higher marginal cost \leftrightarrow Higher quality

$$\log z_j \sim \left(-\frac{1}{2}\sigma_z^2, \sigma_z \right) , \quad \log \phi_j = -\gamma \log z_j , \quad \gamma = 1$$

- Manova, Zhang (QJE, 2012)

- *Firms that export more, and charge higher export prices, import more expensive inputs*

- Hottman, Redding, Weinstein (QJE, 2016)

- *Large role ($\approx 70\%$) for “appeal” differences*

- House of Gucci (2022)

- *High quality, high cost, high price, selling to less price sensitive consumers*